XASP: An Explanation Generation System for Answer Set Programming*

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Abstract. In this paper, we present a system, called xASP, for generating explanations that explain *why* an atom belongs to (or does not belong to) an answer set of a given program. The system can generate all possible explanations for a query without the need to simplify the program before computing explanations, i.e., it works with non-ground programs. These properties distinguish xASP from existing systems such as xClingo, DiscASP, $exp(ASP^c)$, and s(CASP), which also generate explanations for queries to logic programs under the answer set semantics but simplify and ground the programs (the three systems xClingo, DiscASP, $exp(ASP^c)$) or do not always generate all possible explanations (the system s(CASP)). In addition, the output of xASP is insensitive to syntactic variations such as the order conditions and the order of rules, which is also different from the output of s(CASP).

Keywords: Explainable AI, Logic Programming, Answer Set Programming

1 Introduction

Recent interest in explainable artificial intelligence provided the impulse for the development of several systems capable of generating explanations for queries posed to a logic program under the answer set semantics such as xClingo [2], DiscASP [4], $exp(ASP^c)$ [7], and s(CASP) [1]. These systems can be characterized by three dimensions: (*i*) the strategy for computing the explanation (grounding vs. non-grounding), (*ii*) the types of queries that can be posed to the system (true atoms and false atoms), and (*iii*) the representation of the answers. Among these systems, only s(CASP) does not ground the program before computing the answers; both s(CASP) and $exp(ASP^c)$ generate explanations for atoms in an answer set (true atoms) and atoms not in an answer set (false atoms); while xClingo is not applicable to false atoms; and DiscASP currently only works for propositional answer set programs. s(CASP) generates a partial answer set supporting a query while others generate a full justification, represented by an explanation graph, given an answer set.

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2 Ly Ly Trieu, Tran Cao Son, Marcello Balduccini

Grounding a program before computing an explanation comes at some costs. One of the most significant problems is that the grounding simplification techniques applied by answer set solvers tend to remove various pieces of information, resulting in explanations that are no longer faithful to the original program, or unable to even provide an explanation. This is illustrated in the next example.

Example 1 (*Limitation of Current Approaches*). Let *P* be a program:

$$d:=b(X), a(X).$$
 $b(1).$ $a(4).$

This program has a unique answer set $\{a(1), b(4)\}$. *d* is false in this answer set. Suppose that we are interested in the question "why is d false?"

Among the four systems mentioned earlier, only s(CASP) is able to provide an explanation for this query. For other systems, no explanation for a false atom is provided, either by design or by the simplification process. $exp(ASP^c)$ does not return an explanation graph for *d* because *d* is eliminated by the solver during the grounding phase.

In the above example, s(CASP) generates the following justification³

not d :- not b(Var0 | {Var0
$$\geq 1$$
}), b(1), not a(1).

This says that there is an answer set containing b(1), that does not contain a(1) and does not contain any other atom of the form b(x) such that $x \neq 1$.

When we switch the position of b(X) and a(X) in the first rule, we receive a different justification:

not d :- not a (Var0 | {Var0 ≥ 4 }), a(4), not b(4). The above example highlights the shortcomings of existing systems. For *s*(*CASP*), even though both answers are correct, it is not ideal that a slight semantics-preserving change in the input results in a different justification.

In this work, we describe xASP, a system capable of computing the explanation graphs of a ground atom a w.r.t. an answer set A of a non-ground program P. By working directly with programs including variables, xASP generates explanation graphs that are faithful to the program, thus distinguishing itself from xClingo, DiscASP, and $exp(ASP^c)$, which simplify the program before computing an explanation. Different from s(CASP), it generates all full explanation graphs for an atom given an answer set and its behavior is not affected by semantics-preserving changes in the program. To work with programs including variables, xASP uses the given atom and answer set to dynamically identify relevant ground rules for the construction of the answers. Again, the main purpose of xASP is to help respond to the need for explainable AI. However, by presenting the applicable rules, facts, and assumptions used in the derivation of a given atom, xASP could be useful for debugging as well. For example, if an atom a is supposed to be false in all answer sets of a program P but appears in some answer set A, the explanation graph of a could be useful in figuring out which rule must not be applicable, etc.

2 The **xASP** system

xASP generates explanation graphs under the stable model semantics [3]. It deals with normal logic programs, which are collections of rules of the form $h \leftarrow b$ where h is

³ $p(V | V \neq v)$ represents the set of all atoms of the form p(x) except for the atom p(v).

an atom and $b = p_1, \ldots, p_m$, not $n_1, \ldots, not n_s, p_i$ and n_j are atoms, and not is the default negation operator. For a rule r, r^+ and r^- denote the set of positive atoms $\{p_1, \ldots, p_m\}$ and the set of negative atoms $\{n_1, \ldots, n_s\}$, respectively. XASP utilizes the notions of supported set and derivation path [7,8] and the concept of explanation graph [5] which are illustrated using the program P_1 consisting of the following rules:

Given the answer set $A_1 = \{l(1), m, a(4), b(1), k(6)\}$, the explanation graphs of m are shown in Fig. 1. Both indicate that m is true in A_1 because of the existence of the rule r_1 and the following dependencies:

- m depends positively on l(1), which is a fact;
- -m depends negatively on h(1), which is false, because there is only one instance of the rule r_3 with the head h(1). In that instance, h(1) depends positively on k(1)(left) or p (right) and both are false because there is no rule for deriving them;
- m depends negatively on d, which is false. That is because there are two instances of rule r_2 supporting the derivation of d, but none of them is applicable in the given answer set. In fact, both a(1) and b(4) are false because there are no rules for deriving them.

In general, for a node x in an explanation graph G, if x is an atom a then the set of nodes directly connected to a — the nodes y such that $(a, y, _)$ is an edge in G — represents the body of a rule whose head is x and whose body is satisfied by A. If x is $\sim a$ for some atom a, then the set of nodes directly



Fig. 1: Explanation graph of m

connected to $\sim a$ represents a set of atoms whose truth values in A are such to make each rule whose head is a unsatisfied by A. In other words, the direct connections with a node represent the *support* [7] for the node being in (or not in) the answer set under consideration.

The three types of links connecting a node x (corresponding to an atom a) to a node y (for an atom b) in explanation graphs are as follows:

- + (represented by a solid link) demonstrates that the truth value of a depends *positively* on the truth value of b w.r.t. A. If node y is \top (*True*), atom a is a fact.
- - (represented by a dashed link) demonstrates that the truth value of a depends *negatively* on the truth value of b w.r.t. A. If node y is \perp (*False*), it means that atom a is always false. Note that in our prior system $exp(ASP^c)$, this link does not exist because the atoms, that are always false, have been simplified during the grounding process of clingo.
- o (represented by a dotted link) is used in the case in which node y is assume, which means that atom a is assumed to be false (see in examples in [5,7]).

Ly Ly Trieu, Tran Cao Son, Marcello Balduccini



Fig. 2. The overview of xASP system

2.1 Overview of xASP

4

Fig. 2 shows the overview of xASP. The large two boxes represent the two main phases of xASP, grounding as-needed and computing a minimal assumption set. The grey boxes are implemented via $exp(ASP^c)$.

<u>Grounding as-needed</u>: xASP computes the set of ground rules that are necessary for the construction of explanation graphs of a and the set of derivation paths of a given A. It starts by identifying the rules related to a, e.g., rules whose head is a or an atom that a depends on. Afterwards, these rules are grounded, taking into consideration the given answer set. Finally, the derivation paths of a and its dependencies are obtained via the computation of supported sets which is the focus of this paper (Sect. 2.2).

<u>Computing a minimal assumption set</u>: xASP computes E_{TA} , the set of derivation paths of all atoms in the tentative assumption set TA and a minimal assumption set U of A. It then utilizes $exp(ASP^c)$ [7] to construct explanation graphs for a.

2.2 Computing Derivation Paths of a

This section presents a key algorithm for computing E_a , an *associative array* whose keys are a or atoms that a depends on, directly or indirectly, as defined via the dependency graph [6]. $E_a.keys()$ denotes the set of keys in E_a . For each $x \in E_a.keys()$, $E_a[x]$ is the value associated with x in E_a and contains the supported sets of x [7].

Given two atoms $a = p(t_1, t_2, ..., t_n)$ and $b = q(t'_1, t'_2, ..., t'_m)$, we write pu(a, b) to denote that a and b have the same predicates (p = q) and arities (n = m), i.e., a and b are possibly unifiable.

Algorithm 1 takes a grounded atom a and an answer set A of program P as inputs and computes E_a for the construction of the explanation graph for $a \in A$ (true atom) or $a \notin A$ (false atom). E_a is initialized with the empty array (line 1). Only rules in H_a whose head could be unified with a are involved in the partial grounding process (lines 2-14). For each $(h, r^+, r^-) \in H_a$, the grounding process starts with a unifier θ of a and h (line 4). L is the set of



Fig. 3. Explanation graph of d

positive atoms that are not grounded after substituting with θ . $p\theta$ denotes that variables in atom p are substituted by elements in θ . Due to the restriction that variables occurring in negative atoms must appear in positive atoms, ground substitutions of atoms in r^+ are ground substitutions for the negative atoms in r^- . We define $\omega(L, A)$ as the set of potential substitutions for variables in L given A, in which each element θ' of $\omega(L, A)$ is a set of substitutions of the form v/t such that for some $x \in L$ and $x\theta' \in A$, and

Algorithm 1: PartialGrounding(a, P, A)

Input: *a*-a ground atom; *P*-program; *A*-an answer set **Output:** E_a - set of derivation paths of a and a's dependencies 1 Let $E_a[a] = []$ if $a \in A$ or let $E_a[\sim a] = []$ if $a \notin A$ 2 Let $H_a = \{(h, r^+, r^-) \mid r = h \leftarrow b \in P \land pu(a, h)\}$ 3 for $(h, r^+, r^-) \in H_a$ do **if** $\exists ! \theta$ such that θ be the unifier of $\{a, h\}$ then 4 $L = \{p \mid p \in r^+ \land p\theta \text{ is not ground}\}$ 5 for $\theta' \in \omega(L, A)$ do 6 $\theta' \leftarrow \theta' \circ \theta$ // Composition of substitutions 7 $D \leftarrow \{d\theta' \mid d \in r^+\}, N \leftarrow \{n\theta' \mid n \in r^-\}$ 8 if $a \in A$ then 9 $T \leftarrow \{ D \cup \{ \sim n \mid n \in N \} \mid D \subseteq A, N \cap A = \emptyset \}$ 10 Append T to $E_a[a]$ 11 else 12 $T \leftarrow \{\{d\} \mid d \in A \cap N\} \cup \{\{\sim n\} \mid n \in D \setminus A\}$ $E_a[\sim a] \leftarrow [X \cup L \mid X \in E_a[\sim a], L \in T]$ 13 14 15 $E_a[\sim a] \leftarrow [\{\bot\}] \mid \nexists(h, r^+, r^-) \in H_a$ such that a is unifiable with h 16 PartialGrounding(c, P, A) where either $c \in C$ or $\sim c \in C, C \in E_a[a] \cup E_a[\sim a]$ 17 return E_a

 $\{v \mid v/t \in \theta'\} = V$ where V is the set of variables in L. Note that θ' must be composed to a valid substitution for variables in L, e.g., it must not specify two different values for a variable (called conflict in the variable). In addition, some atoms in L cannot be unified with any atoms in A and hence are false w.r.t. A. Therefore, those atoms are not grounded (see Sect. 2.3). If $L = \emptyset$, $\omega(L, A)$ is empty. After obtaining substitutions, the positive and negative atoms are grounded via θ' (line 7) and supported sets of a are computed which depend on the truth value of a in A (lines 6-14). Note that, in line 10, if $D = \emptyset$ and $N = \emptyset$, then $T = \{T\}$, denoting that atom a is a fact. Observe that if there are no rules whose head can be unified with a, then the atom is false (no rule in P supports a). As such, $E_a[\sim a]$ is set to $[\{\bot\}]$, i.e. atom a is false in P (line 15). Unlike $exp(ASP^c)$, Alg. 1 is recursively called only on atoms in supported set of a (line 16).

Example 2. Let us reconsider program P_1 and compute the derivation paths for m. Given a ground atom m, there is only rule r_1 whose head is unifiable with m where $\theta = \emptyset$. θ is not a ground substitution for positive atoms in r_1 . Thus, answer set A_1 is utilized to obtain a unifier $\{X/1\}$ to substitute for atoms in the body of r_1 , resulting in $E_m[m] = \{l(1), \sim d, \sim h(1)\}$. Alg. 1 is called recursively on atoms l(1), d and h(1).

 $- E_m[l(1)] = [\{\top\}]$ because of rule r_6 .

- Similar to m, unifier $\theta = \emptyset$ for atom d is not a ground substitution for positive atoms in r_2 . However, given A_1 , we can conclude that there are two possible substitutions, $\{X/1\}$ and $\{X/4\}$, for r_2 . We have $E_m[\sim d] = [\{\sim a(1), \sim b(4)\}]$. Alg. 1 is then called for atoms a(1) and b(4).

• Although the head of rule r_5 has the same predicate and arity as a(1), a(1) and a(4) are not unifiable. Thus, $E_m[\sim a(1)] = [\{\bot\}]$. Similar to a(1), $E_m[\sim b(4)] = [\{\bot\}]$.

Ly Ly Trieu, Tran Cao Son, Marcello Balduccini

- Similally, we have $E_m[\sim h(1)] = [\{\sim k(1)\}, \{\sim p\}], E_m[\sim k(1)] = [\{\bot\}]$ and $E_m[\sim p] = [\{\bot\}].$

2.3 Illustrations

6

Fig. 3 shows the explanation graph for d in the case of Example 1. Unlike *s*(*CASP*), in XASP the explanation for d being false is that all possible ground rules whose head is d have an unsatisfied body, in this case because a(1) and b(4) are false.

Consider another program P' containing the rules:

 (r_1) m :- not q. (r_2) q :- d(X). (r_3) d(X) :- a(X), 1. (r_4) a(1).

An explanation graph of m w.r.t. P' and answer set $A' = \{m, a(1)\}$ is shown in Fig. 4. It contains non-ground atom d(X) because no atoms formed by d/1 occur in A'.



m

3 Conclusion

Fig. 4. Explanation graph of m

We presented xASP, a system for computing explanation graphs of true and false atoms w.r.t. an answer set of a program. xASP does not simplify the program before finding the explanations, thus providing faithful explanations for the truth value of the given atom. This is important to form a correct understanding of programs. Future work includes testing xASP on realistic debugging tasks and supporting the full language of clingo.

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